

COMPUTATIONAL SIMULATION OF AN IF-STEEL DEFORMED BY EQUAL CHANNEL ANGULAR PRESSING VIA THE FINITE ELEMENT METHOD

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Abstract: The objective of this work is to evaluate the equivalent plastic strain levels induced by equal channel angular pressing (ECAP) in an IF-steel billet after one pass at room temperature using the finite element method (FEM). For this purpose two-dimensional models were developed using a plane strain condition. It can be concluded that the simulation of this ultra-low carbon steels be interpreted as a quasi-static process because accurate results were observed in comparison to the analytical models reported in the literature.

Key-words: ECAP, severe plastic deformation, FEM, IF steel.

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1. INTRODUCTION

The processing of nanostructured materials by mean of severe plastic deformation methods (SPD) has attracted a great scientific interest, mainly by the advantages of the SPD materials in comparison to other nanostructured materials ⁽¹⁾. Special metal forming methods were developed and used to this finality. One of the most prospective candidate for many practical applications is the equal channel angular pressing (ECAP) ⁽²⁾. This method was invented by Segal ^(3, 4) and is upon the of the simple shear strain-path in the optimization of some metal forming operations ^(5, 6). In this method a well lubricated billet is extruded by a plunger through a special die. Machined with two channels of constant cross-section, which intersect angle Φ is generally 90° . The principle of the ECAP method is schematically shown in Figure 1 ⁽⁷⁾. In this figure, the angle Ψ defines the outer curvature of the intersection between the two channels.

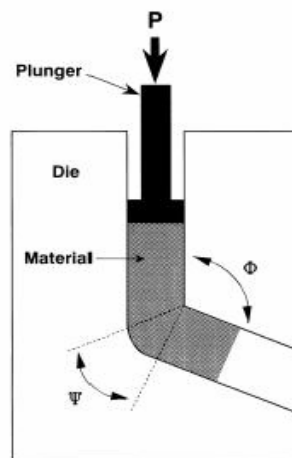


Figure 1. Schematic view of the equal channel angular pressing (ECAP) method ⁽⁷⁾.

The ECAP is a very interesting method provided that the billet has no significant shape changes and the accumulated plastic strains are very high in comparison to the traditional metal forming operations, such as the cold rolling and the drawing processes. Therefore, the comprehension of the mechanics of deformation occurring during the ECAP process is very important so as to evaluate the microstructure and the grain refinement attained as a

function of the deformations routes. In this context, the use of the extreme principles, for instance, the upper bound method has gained a lot of attention to estimate the pressure needed for the plunger as well as the accumulated effective strain resulting from the ECAP method^(8, 17, 18). In addition, the numerical simulation with the help of the finite element method (FEM) has been extensively used to better understating the ECAP method⁽⁹⁻¹⁴⁾.

In the present work, a quasi-static solution to the ECAP method by the FEM simulation was carried out using dies with intersecting angles $\Phi = 90^\circ$ and 120° , considering only one pass of extrusion and adopting a plane strain state. A frictionless condition was used to compare the effective strain and extrusion force obtained by FEM and those predicted by upper bound solution. In addition, values of 0.05 and 0.1 to the friction coefficient were adopted to study the development of the uniform plastic strain zone. In all cases, the generalized Coulomb law was assumed.

2. ANALYTICAL SOLUTIONS OF THE EFFECTIVE PLASTIC STRAIN AND EXTRUSION PRESSURE

Iwahashi and et al.⁽⁸⁾ have proposed a relationship between effective strain, ε_{eff} , and the ECAP angles Φ and Ψ . This expression is calculated from von Mises isotropic yield criterion applied to the pure shear condition as:

$$\varepsilon_{\text{eff}} = \frac{N}{\sqrt{3}} \left[2 \cot \left(\frac{\Phi}{2} + \frac{\Psi}{2} \right) + \Psi \cos ec \left(\frac{\Phi}{2} + \frac{\Psi}{2} \right) \right] \quad (1)$$

where N the number of the extrusion passes. Here, to $N = 1$ and $\Psi = 0^\circ$, equation (1) reduces in the previously relation obtained by Segal⁽⁶⁾:

$$\varepsilon_{\text{eff}} = \frac{2}{\sqrt{3}} \left[\cot \left(\frac{\Phi}{2} \right) \right] \quad (2)$$

Alkorta *et al.* ⁽¹⁷⁾ proposed an upper bound solution to the ECAP pressure considering Hollomon-type materials and using a frictionless condition. According to these authors, the pressure is related with the material hardening behavior as follows:

$$P_{ECAP} = \left(\frac{\sigma_0}{n+1} \right) \left[\frac{2 \cot \left(\frac{\Phi + \Psi}{2} \right) + \Psi}{\sqrt{3}} \right]^{(n+1)} \quad (3)$$

where σ_0 and n are the yield stress and the strain-hardening exponent, respectively.

Based in this study, an analogue ECAP pressure solution considering a Swift-type material is adopted in the present work, $\bar{\sigma} = K(\varepsilon_0 + \bar{\varepsilon}^p)^n$, where K is the strength coefficient, ε_0 is the pre-strain and $\bar{\varepsilon}^p$ is effective von Mises plastic strain. Thus, considering a single extrusion pass, the equation (3) becomes:

$$P_{ECAP} = \left(\frac{K}{n+1} \right) \left\{ \left[\left(\frac{\sigma_0}{K} \right)^{\left(\frac{1}{n} \right)} + \frac{2 \cot \left(\frac{\Phi + \Psi}{2} \right) + \Psi}{\sqrt{3}} \right]^{(n+1)} - \left[\left(\frac{\sigma_0}{K} \right)^{\left(\frac{1}{n} \right)} \right]^{(n+1)} \right\} \quad (4)$$

The extrusion force per unit of thickness, after a single extrusion pass, can be obtained multiplying the right side of the equation (4) by the width (W) of the billet. Thus,

$$\frac{F_{ECAP}}{thickness} = W \left(\frac{K}{n+1} \right) \left\{ \left[\left(\frac{\sigma_0}{K} \right)^{\left(\frac{1}{n} \right)} + \frac{2 \cot \left(\frac{\Phi + \Psi}{2} \right) + \Psi}{\sqrt{3}} \right]^{(n+1)} - \left[\left(\frac{\sigma_0}{K} \right)^{\left(\frac{1}{n} \right)} \right]^{(n+1)} \right\} \quad (5)$$

The F_{ECAP} calculations were carried out through a computational code developed in Fortran language. A billet of 50 mm (height) x 10 mm (width) and unitary thickness is considered. The material analyzed in this work is an IF steel which is described in uniaxial tension by $K = 544.96$ MPa, $\varepsilon_0 = 0.004852$ and $N = 0.235$, according to reference (21).

3. THE FINITE ELEMENT ANALYSIS

The simulation of the extrusion of the IF steel billet was made by assuming isothermal conditions at room temperature and neglecting the heating conditions due to the friction between the workpiece and the die tool. The numerical simulations were performed with commercial finite element code ANSYS. The details of the FEM modeling are described as follows.

3.1 *Modeling of the die*

Two distinct models for the ECAP die were developed. One considering the channels intersection angle $\Phi = 90^\circ$ and another $\Phi = 120^\circ$. In both cases, the angle Ψ was assumed to be zero. The dies were assumed to be rigid pieces and the material used was an H13 tool-steel with the Young modulus E and the Poisson's ratio ν equal to 200,000 MPa and 0.3 respectively.

The details of the channels are shown in Figure 2. It can be noted the presence of a curvature radius of 1.5 mm at the top channels intersection. It was necessary to the convergence of the solution, according to Luis-Pérez⁽¹⁹⁾. The choice of this particular die geometry is in agreement with the ECAP design in progress in the Laboratory of Mechanical Tests at the Federal Fluminense University (EEIMVR/UFF).

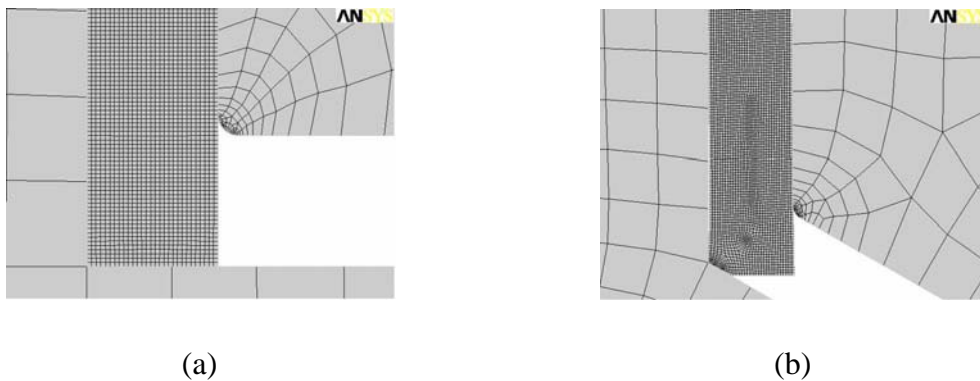


Figure 2. Details of the two-dimensional ECAP die tooling FEM modeling: (a) intersection angle $\Phi = 90^\circ$ and (b) intersection angle $\Phi = 120^\circ$.

3.2 *Modeling of the billet*

The two-dimensional workpiece considered has the dimensions of 10 mm (width) x 50 mm (height) and a unity thickness since a plane-strain condition is assumed.

The material of the billet was assumed to be isotropic elastic-plastic and its elastic properties were $E = 195,000$ MPa and $\nu = 0.29$ whereas the plasticity is defined by the von Mises or J2 associated flow rule. The billet is described by 4,590 linear four-node plane-strain elements, PLANE 182 according to the ANSYS terminology⁽¹⁶⁾.

3.3 *Loadings and workpiece-tooling contact*

The plunger is not taking into account the finite element modeling. It has been replaced by a displacement boundary condition imposed to the top nodes of the billet as shown in Figure 3. In order to assure the quadratic convergence of the Newton-Raphson method used in the ANSYS code, the top billet displacements were fixed in increments of 0.25 mm up to a total displacement of 45 mm.

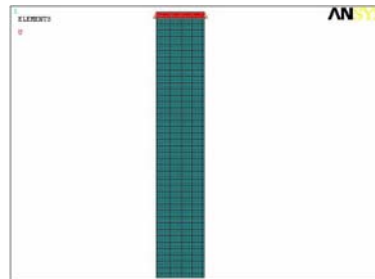


Figure 3. Boundary displacements applied on the top nodes of the billet, represented by the red symbols.

Concerning the friction behavior at the workpiece-tooling interface, the friction coefficient values of 0, 0.05 and 0.1 were attributed at the models to carry out the simulations. To represent the friction behavior, the generalized Coulomb's law was used in the FEM models.

How known, the generalized Coulomb's law states a relation between yield stresses in pure shear and uniaxial tension, respectively. Specifically in the Ansys program, this relation is verified by mean of von Mises yield criterion corrected to pure shear condition and is given by:

$$\tau_{MAX} = \frac{\sigma_Y}{\sqrt{3}} \quad (6)$$

where τ_{MAX} and σ_Y are the yield stresses in pure shear and uniaxial tension, respectively. Thus, to stress values lesser than τ_{MAX} , sliding of the workpiece is observed and to higher or equal values of τ_{MAX} , an adherence condition has occurred, like a weld.

Finally, a flexible contact between workpiece and tool was employed. For this step, CONTA 171 ⁽¹⁹⁾ and TARGE 169 ⁽¹⁹⁾ elements have been used. The contact regions assumed were in relation of the billet, it left, right and bottom sides and to the dies the contact regions were the channel lines next to the billet. Figure 4 shows these contact regions. There, only bottom portions of the models are shown and the coarse black and blue lines represent the contact considered to each die configuration. The contact status was updated after each load step to avoid inaccurate results. Thus, taking in account the die geometries considered, the total time spent in the simulations does not exceed 6 hours, using a Pentium IV computer with 4GB of RAM memory.

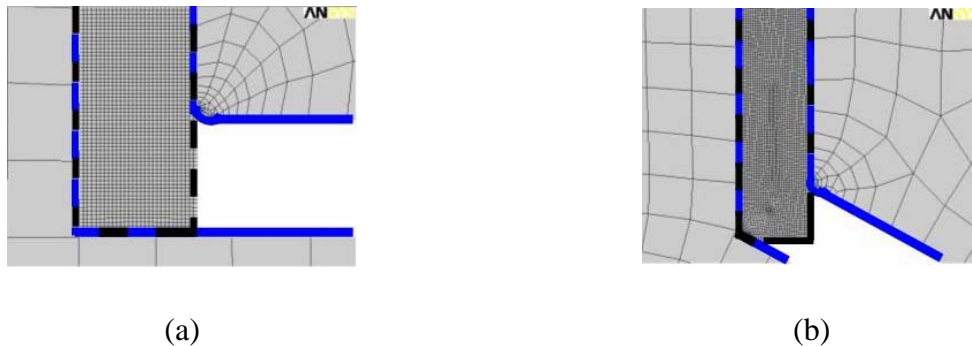


Figure 4. Details of the contact workpiece-tool; (a) contact regions to 90° die; (b) contact regions to 120° die. The black coarse traced lines refer to billet contact and blue coarse traced lines refer to die contact regions.

4. RESULTS AND DISCUSSIONS

4.1 Extrusion force and effective strain obtained by the upper bound method and FEM: frictionless condition

In the absence of the friction, the extrusion force per unit of thickness obtained from equation (5) is greater than FEM simulations in both $\Phi = 90^\circ$ and 120° , as shown in Figure 5(a). Besides, the force increases with decreasing Φ angles as reported in the literature⁽¹⁷⁻²⁰⁾. The FEM results presented in Figure 5(a) represent an average value obtained from regions AB ($\Phi = 90^\circ$) and CD ($\Phi = 120^\circ$), where the ECAP force has reached a steady-state condition, see Figure 5(b). The distinct behavior of these curves can be explained by the fact of the normal pressure at 90° is greater than at 120° due to the bending-unbending effect, which is more important in the first case.

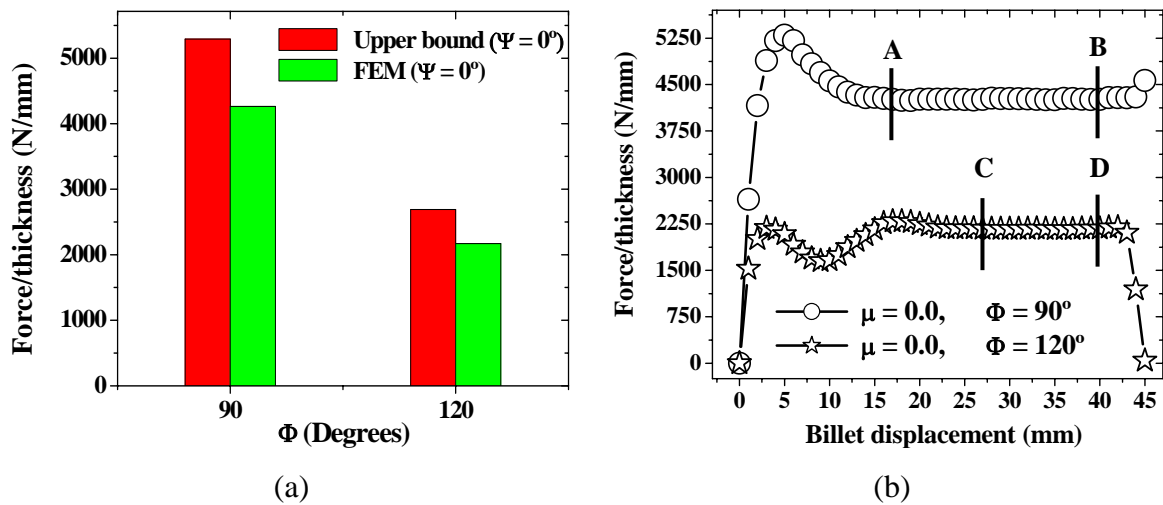


Figure 5. (a) comparison between upper bound and FEM extrusion forces; (b) extrusion force vs. displacement on the billet, illustrating the regions of average values used in (a).

A decrease of the Φ angle is directly linked to the attainment of higher effective plastic strains. This is confirmed in Figure 6 wherein the FEM values were calculated by averaging the nodal results in the path traced along the homogeneous strain zone, obtained after 45 mm

of the billet displacement. The paths used in both die configurations to obtain the effective plastic strains are represented in Figure 7 by black arrows where its limits are delimited by nodes I and J depicted by black dots.

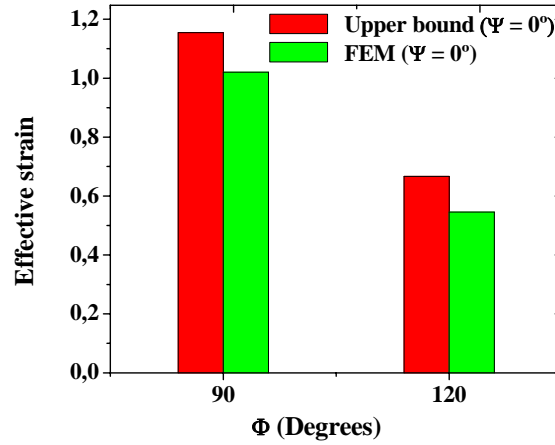


Figure 6. Comparison between the upper bound and FEM predictions of the effective plastic strains obtained for $\Phi = 90$ and 120 degrees.

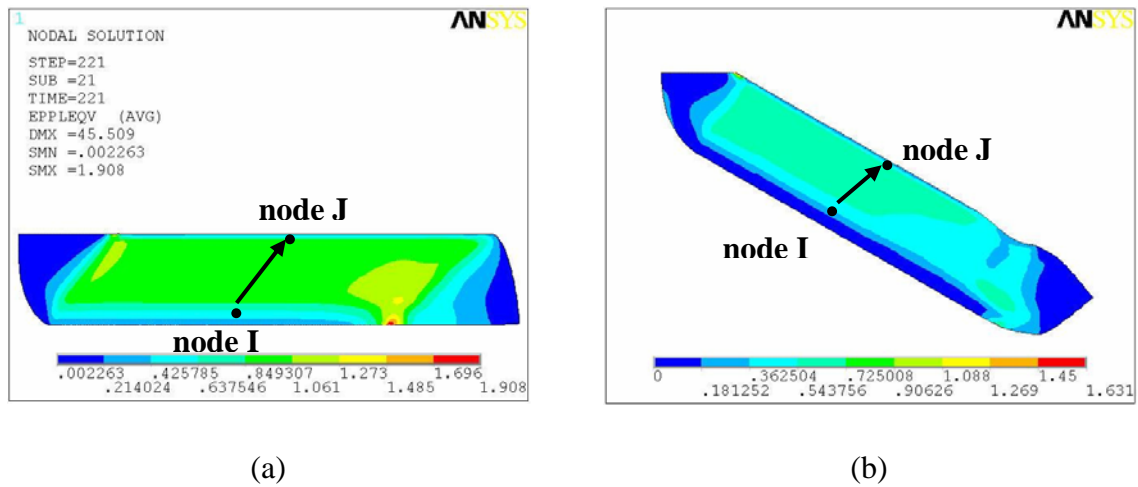


Figure 7. Procedure to obtain the average values for the effective plastic strains: (a) $\Phi = 90^\circ$; (b) $\Phi = 120^\circ$.

4.2 Friction stresses and effective plastic strains as a function of the μ -value

The appearance of a shear plane at 45° between the two channels is independent of the friction condition as well as of the intersection angle Φ . Figure 8 presents the numerical predictions for the friction stress and the contact pressure as a function of the μ -value

obtained for $\Phi = 90^\circ$ from the nodes located at the left and right billet sides. It is worth to note an inversion of the friction stresses sign which is attributed to the passage of the billet towards the second channel. Also, either the friction stress or the contact pressure increases with the friction coefficient and, in particular, higher μ -values provide a sticking friction condition as observed at the billet right side for displacement $U_y = 20$ mm. This explains the outlet inwards rounded shape of the billet, as shown in Figure 7(a).

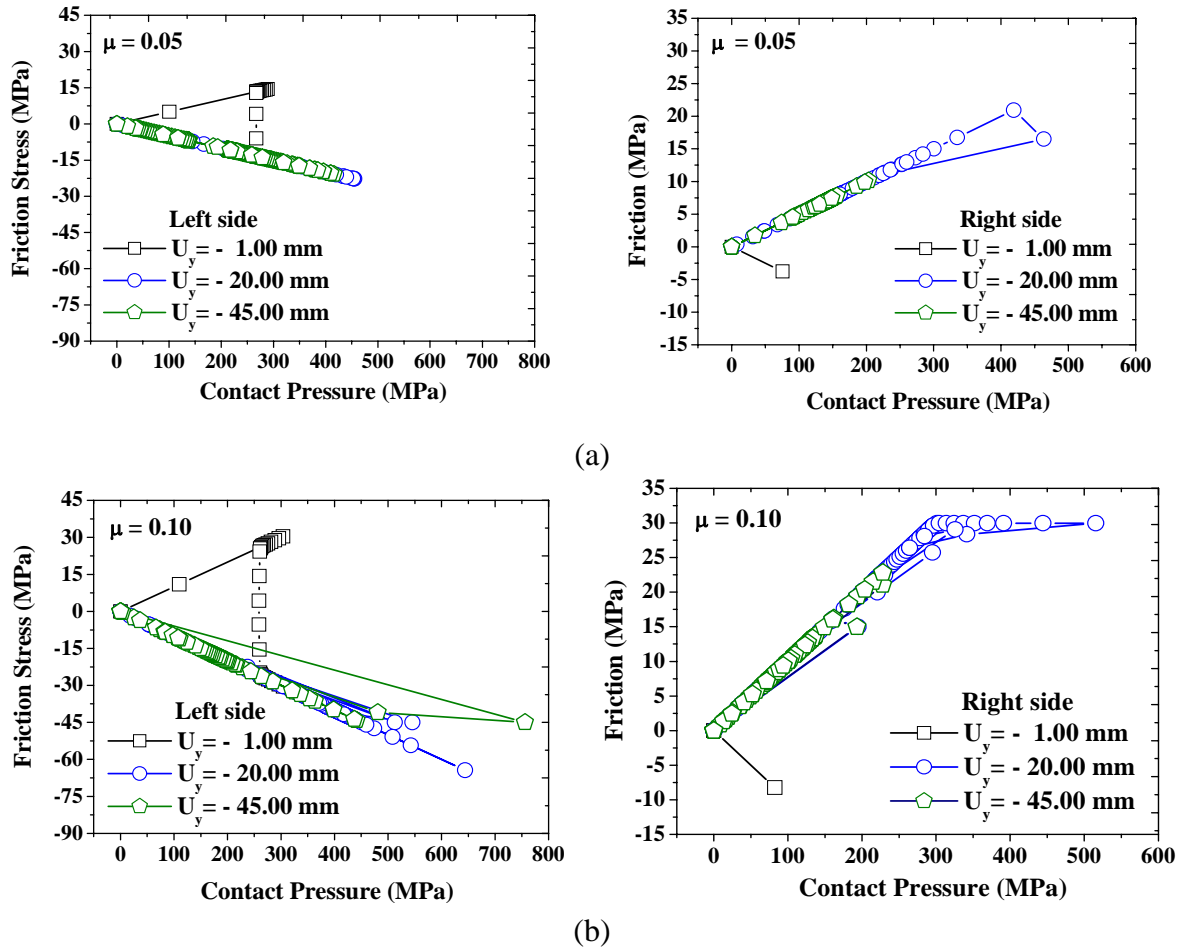


Figure 8. Friction stress and die contact pressure obtained for $\Phi = 90^\circ$ from the nodal values located at the left and billet right sides: (a) $\mu = 0.05$ and (b) $\mu = 0.10$.

On the other hand, Figure 9 compares the reaction nodal forces determined for $\Phi = 90^\circ$ and 120° as a function of the μ -value and the billet displacement. As expected, the increasing in the friction coefficient requires higher extrusion pressures or punch loads. Also, it can be observed an increase of the reaction forces up to about 7.5 mm and 5 mm for the intersecting

angles $\Phi = 90^\circ$ and $\Phi = 120^\circ$ respectively followed by a decreasing up to about 10 mm, which corresponds to the channels width, which is due to the first bending of the billet edge. For $\Phi = 90^\circ$, a common initial behavior is observed for all the extrusion forces with a peak, due to the inwards rounded shape of the billet as shown in Figure 10(a), followed by an immediate unloading caused by the inversion of the shear stresses sign. Next, a progressive and approximately linear increasing of the nodal extrusion force is noted when $\mu = 0.05$ whereas there is a drop for $\mu = 0.10$ due to the adherence of the billet right side at the second channel. Conversely, the force evolution obtained for $\Phi = 120^\circ$ shows a reloading up to 15 mm due to the second bending needed to complete the rotation of the billet, see Figure 10 (b).

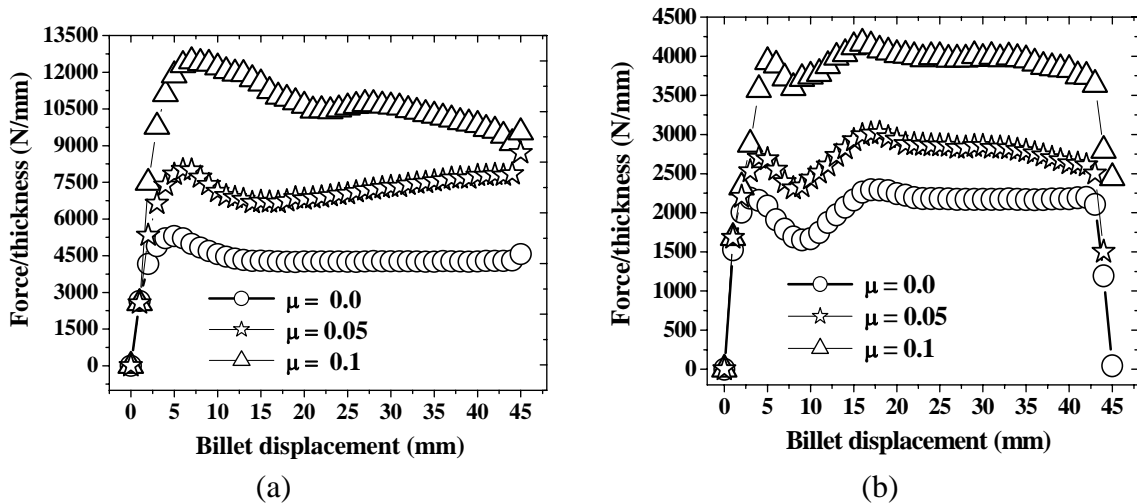


Figure 9. Extrusion forces in function of the friction conditions: (a) $\Phi = 90^\circ$; (b) $\Phi = 120^\circ$.

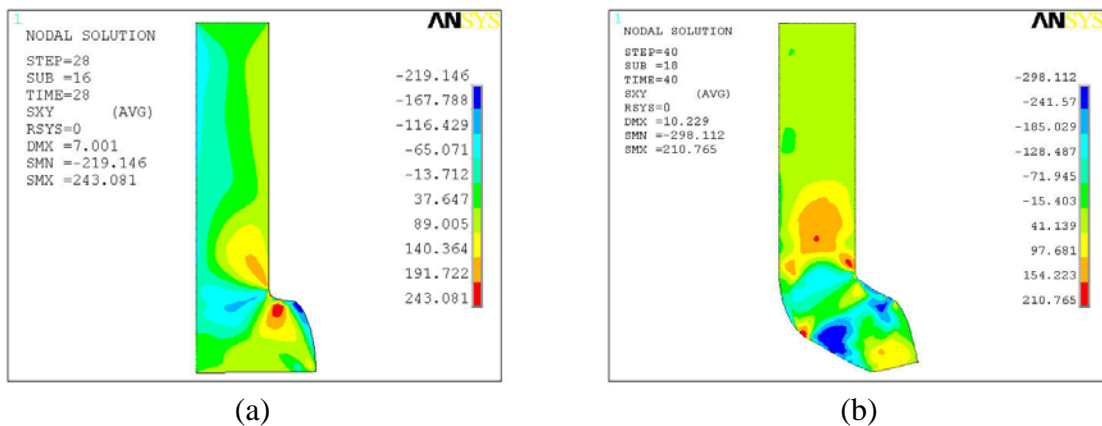


Figure 10. Shear stress distributions obtained for $\mu = 0.10$: (a) $\Phi = 90^\circ$ at $U_y = 7$ mm and (b) $\Phi = 120^\circ$ at $U_y = 10$ mm.

Figure 11 shows the iso-contours plots of the effective von Mises plastic strains and stresses determined for $\Phi = 90$ and $\mu = 0.05$. Firstly, one can observe that either the bottom or the top of the billet present the smallest effective strains since these regions do not cross the 45° shear zone between the two channels. Secondly, the extremely high value of the effective plastic strain close to 2.4 is due to process condition $\Psi = 0$ which leads to the mesh folding. Furthermore, the uniform regions of the effective plastic strains are originated by the stress flow lines normal to the direction of the displacements application, as previously reported by Kim *et al.* ⁽⁹⁾. Finally, it should be important to note that the strain-hardening curve obtained in an uniaxial test have a great limitation in the case of SPD simulations, where the $\epsilon_{\text{eff}} \gg 1$, since the maximum von Mises plastic stress value observed in Figure 11(b) corresponds approximately to the K-value for the IF steel in the Swift strain-hardening curve. Therefore, more appropriate results should be obtained by the use of a strain-hardening curve from pure shear experiments, for instance, by means of torsion tests. In this case, one should apply the plastic work equivalence principle so as to convert the strain-hardening curve determined from the torsion experiment to an effective stress-strain curve to be used in the numerical simulations of the ECAP process.

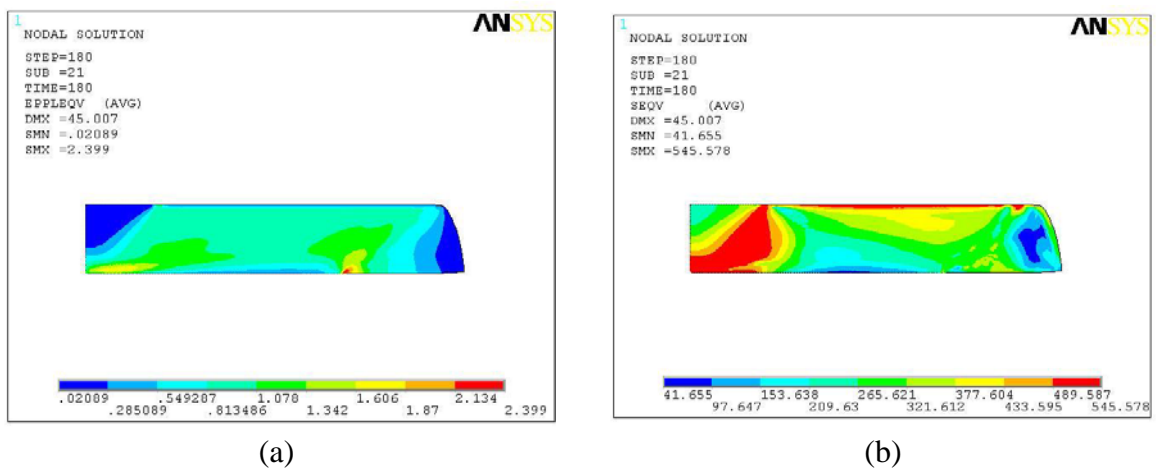


Figure 11. (a) Effective plastic strains obtained after a 45 mm of billet displacement with $\mu = 0.05$ and $\Phi = 90^\circ$ and (b) correspondent von Mises effective stresses.

5. CONCLUSIONS

The results obtained from the theoretical and FEM predictions for a single pass extrusion of an IF steel billet in an equal channel angular die can be summarized as follows:

1. The analytical upper bound solution for a Swift-type material provided higher working loads and effective plastic strains values in comparison to the FEM results obtained from a plane-strain model.
2. The FEM simulations revealed the existence of a shear plane at 45° for either intersecting angles Φ (90° and 120°), which occurs independently of the friction condition between the billet and the die. In fact, this can be attributed it to the higher contact pressure on the outer region of the die. Moreover, the friction conditions have a great influence upon the extrusion loads and effective plastic strains, mainly for $\Phi = 90^\circ$. Conversely, the friction influence on the effective strain is less important for $\Phi = 120^\circ$, as reported in the literature.
3. The adoption of the true-stress true-strain hardening curve obtained from uniaxial tests permits a relatively accurate analysis of the ECAP for ductile materials such as the IF steel. However, in order to better analyze the effective plastic strains induced in two or more passes, one should employ the strain hardening curve determined from pure shear experiments, wherein the accumulated plastic strains greater than 1 can be accomplished as well as the plane-strain condition can be assured.

6. ACNOWLEDGEMENTS

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